# Theoretical Investigations of the EPR Parameters for Three Tetragonal Centers in CsCl:Cr<sup>3+</sup> Crystal

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The electron paramagnetic resonance parameters zero-field splitting D and g factors  $g_{\parallel}$  and  $g_{\perp}$  of three tetragonal centers in CsCl:  $\operatorname{Cr}^{3+}$  crystal at room temperature have been investigated by a two-spin-orbit (S. O.)-coupling parameter model. In this model, the contributions arising from the S. O. coupling of the central  $d^3$  ion and the ligands are included. For center III, the very small D of the  $[\operatorname{CrCl}_6]^{3-}$  cluster may be due to the displacement ( $\approx 0.506\,\text{Å}$ ) of the two substitutional  $\operatorname{Cl}^-$  ions along the tetragonal ( $C_4$ ) axis. For the centers I and II, the relatively larger D results from the contribution of two or one water molecules, i.e., corresponding to  $[\operatorname{CrCl}_{6-n}(\operatorname{H}_2\operatorname{O})_n]^{n-3}$  with, n=2 or 1 along the  $C_4$  axis, respectively. The reasonableness of the theoretical results is discussed.

*Key words:* Electron Paramagnetic Resonance (EPR); Crystal and Ligand-Field Theory; Cr<sup>3+</sup>; CsCl.

## 1. Introduction

Electron paramagnetic resonance (EPR) and optical studies [1,2] on CsCl:Cr<sup>3+</sup> crystals at room temperature have shown that Cr<sup>3+</sup> occupies an interstitial site in the plane of four Cl<sup>-</sup> (see Fig. 4 of [1]), and that the two host  $Cs^+$  along the [001] (or  $C_4$ ) axis may be substituted by Cl<sup>-</sup> ions or water molecules due to charge compensation, and so the local symmetry of Cr<sup>3+</sup> is tetragonal. In fact three tetragonal Cr<sup>3+</sup> centers, named I, II and III, were found in the EPR measurements [1]. For center III, the very small zero-field splitting D ( $|D| \approx 25 \times 10^{-4} \text{ cm}^{-1}$ ) is attributed to an incorporated [CrCl<sub>6</sub>]<sup>3-</sup> cluster, as supported by the optical studies in Refs. [2-5]. In contrast, associated with the  $[CrCl_{6-n}(H_2O)_n]^{n-3}$  cluster for n = 2 or 1, the relatively larger D is attributed to the center I ( $|D| \approx$  $2170 \times 10^{-4} \text{ cm}^{-1}$  [1]) or II ( $|D| \approx 1400 \times 10^{-4} \text{ cm}^{-1}$ [1]), respectively. However, until now no satisfactory theoretical analysis has been made on the above three centers. In this paper, the EPR parameters D,  $g_{\parallel}$  and  $g_{\perp}$ for the three tetragonal Cr3+ centers are reasonably explained based on a two-spin-orbit-coupling parameter model.

## 2. Theory and Calculation

For transition-metal  $(3d^n)$  ions in crystals, theoretical investigations of the EPR parameters can be made

by using Macfarlane's high-order perturbation methods [6,7] when the S.O. coupling parameter of ligands is smaller than that of central metal ions. However for CsCl:Cr<sup>3+</sup> crystal, where the S.O. coupling parameter  $(\approx 587 \text{ cm}^{-1} \text{ [8]})$  of the ligands is much larger than that ( $\approx 240 \text{ cm}^{-1}$  [9]) of the central Cr<sup>3+</sup> ion, the contribution from S.O. coupling of the ligands cannot be neglected. So, in the study of the EPR parameters of the CsCl:Cr<sup>3+</sup> crystal made in this paper the conventional perturbation formulas of D,  $g_{\parallel}$  and  $g_{\perp}$  for the 3d<sup>3</sup> ion in tetragonal symmetry including only the contribution of the central d<sup>3</sup> ion should be replaced by two-S.O.-parameter formulas containing the contributions from both the central 3d<sup>3</sup> ion and that of the ligands. This point has been supported by some authors [10, 11].

For  $3d^3$  ions in tetragonal symmetry, the two-S.O.-coupling parameter formulas of D,  $g_{\parallel}$  and  $g_{\perp}$  can be expressed as [12]

$$D = \frac{35}{9}D_{t}\zeta'^{2}[1/E_{1}^{2} - 1/E_{3}^{2}] - 35BD_{t}\zeta\zeta'/E_{2}E_{3}^{2},$$

$$g_{\parallel} = g_{s}\frac{8k'\zeta'}{3E_{1}} - \frac{2\zeta'}{9E_{1}^{2}}(2k'\zeta - k\zeta' + 2g_{s}\zeta')$$

$$+ \frac{4\zeta'^{2}}{9E_{3}^{2}}(k - 2g_{s}) - \frac{2\zeta^{2}}{3E_{2}^{2}}(k + g_{s})$$

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$$+ \frac{4k'\zeta'\zeta}{9E_{1}E_{3}} - \frac{4k'\zeta'\zeta}{3E_{1}E_{2}} + \frac{4k'\zeta'\zeta}{3E_{2}E_{3}} + \frac{140k'\zeta'D_{t}}{9E_{1}^{2}},$$

$$g_{\perp} = g_{\parallel} - 210k'\zeta'D_{t}/9E_{1}^{2}, \tag{1}$$

where

$$\zeta = N_{t}(\zeta_{d}^{0} + \lambda_{t}^{2}\zeta_{p}^{0}/2),$$

$$\zeta' = (N_{t}N_{e})^{1/2}(\zeta_{d}^{0} - \lambda_{t}\lambda_{e}^{2}\zeta_{p}^{0}/2),$$

$$k = N_{t}(1 + \lambda_{t}^{2}/2),$$

$$k' = (N_{t}N_{e})^{1/2}(1 - \lambda_{t}\lambda_{e}/2).$$
(2)

and  $g_s(=2.0023)$  is the spin-only value.  $\zeta_d^0$  and  $\zeta_p^0$  are, respectively, the S.O. coupling parameters of the d electron of the central ion and that of the p electron of the ligand in free state. For CsCl:Cr<sup>3+</sup> crystal under study,  $\zeta_d^0 \approx 240 \text{ cm}^{-1}$  [9] and  $\zeta_p^0 \approx 587 \text{ cm}^{-1}$  [8].  $D_t$  is the tetragonal field parameter.  $E_i$  are the zero-order energy separations between the ground  $^4A_2$  and the excited  $^4T_2$ ,  $^2T_{2a}$ , and  $^2T_{2b}$  states [12].  $N_\gamma$  and  $\lambda_\gamma$  are the normalization factor and the orbital mixing parameter, which can be obtained from the approximate relationship [12]

$$f_{\gamma} = N_{\gamma}^2 [1 + \lambda_{\gamma}^2 S_{\rm dp}^2(\gamma) - 2\lambda_{\gamma} S_{\rm dp}(\gamma)], \tag{3}$$

and the normalization relationship [12]

$$N_{\gamma}(1 - 2\lambda_{\gamma}S_{\rm dp}(\gamma) + \lambda_{\gamma}^2) = 1, \tag{4}$$

where  $S_{dp}(\gamma)$  is the group overlap integral and  $f_{\gamma}$  [ $\approx$   $(B/B_0 + C/C_0)/2$ ] the ratio of the Racah parameters for an ion in a crystal to that in free state.

## 2.1. Center III

From the optical spectra of CsCl: $Cr^{3+}$  crystals at room temperature [2], one can obtain the cubic field parameter Dq and the Racah parameters B and C for center III (or  $[CrCl_6]^{3-}$  cluster):

$$D_{\rm q} \approx D_{\rm q} (Cl^-) \approx 1370 \, {\rm cm}^{-1},$$
  $B \approx 645 \, {\rm cm}^{-1}, C \approx 2920 \, {\rm cm}^{-1}.$  (5

According to the Racah parameters  $B_0 \approx 920 \, \mathrm{cm}^{-1}$  and  $C_0 \approx 3331 \, \mathrm{cm}^{-1}$  [9] for a free  $\mathrm{Cr}^{3+}$  ion, we have  $f_\gamma \approx 0.7899$ .

By using the superposition model [14], the tetragonal field parameter for center III can be written as

$$D_{\rm t} \approx \frac{16}{21} \bar{A}_4({\rm Cl}^-)[(R_0/R_\perp)^{t_4} - (R_0/R_\parallel)^{t_4}],$$
 (6)

where  $R_{\parallel}$  and  $R_{\perp}$  are the Cr<sup>3+</sup>-Cl<sup>-</sup> distances parallel and perpendicular to the  $C_4$  axis, respectively. The reference bonding distance  $R_0 \approx \bar{R} = (R_{\parallel} + 2R_{\perp})/3$ . For the ionic crystal, similar to the point-charge model, we take the power law exponent  $t_4 \approx 5$  [14, 15]. The intrinsic parameter  $\bar{A}_4(Cl^-)$  for the hexachloro-complex can be obtained from the relationship  $\bar{A}_4$  (Cl<sup>-</sup>)  $\approx$  (3/4)  $D_{\rm q}$  [15]. For simplicity we consider  $R_{\perp}$  to be the sum of the ionic radii of  $Cr^{3+}$  ( $r \approx 0.755 \text{ Å}$  [16]) and the coplanar Cl<sup>-</sup> ( $r \approx 1.81 \text{ Å [17]}$ ), i. e.,  $R_{\perp} \approx 2.565 \text{ Å}$ . As for  $R_{\parallel}$ , if the two substitutional Cl<sup>-</sup> ions occupy exactly the host Cs<sup>+</sup> sites, the sum of the ionic radii of Cr<sup>3+</sup> and the substitutional Cl<sup>-</sup> is 2.565 Å, even larger than half of the lattice constant ( $a \approx 4.11 \text{ Å [1]}$ ) of CsCl. So, the two substitutional Cl<sup>-</sup> ions may be expected to be displaced away from the central interstitial  $Cr^{3+}$  ion by about an amount  $\Delta Z$  due to the spacial size effect along the  $C_4$  axis, in spite of the electrostatic attraction between the central Cr<sup>3+</sup> and the two  $Cl^-$  along  $C_4$  axis. By fitting the observed of D, we find that for center III

$$\Delta Z \approx 0.506 \,\text{Å} \quad \text{or} \quad R_{\parallel} \approx 2.561 \,\text{Å}.$$
 (7)

Thus, we have the average metal-ligand distance  $\bar{R}=(R_{\parallel}+2R_{\perp})/3\approx 2.564$  Å. By using the Slater-type SCF function [18,19] and the value of  $\bar{R}$ , the group overlap integrals  $S_{\rm dp}(t_{2g})\approx 0.01555$  and  $S_{\rm dp}(e_g)\approx 0.05$  can be obtained, and the parameters  $N_{\gamma}$  and  $\lambda_{\gamma}$  can be also calculated. In consideration of the tetragonal field parameter  $D_{\rm t}~(\approx -6.1~{\rm cm}^{-1})$ , from (6), one may reasonably suggest that for center III the tetragonal distortion is very small, which also agrees with its experimental D value. The related theoretical D,  $g_{\parallel}$  and  $g_{\perp}$  are shown in Table 1.

## 2.2. Centers I and II

According to the larger values of centers I and II [1], and the superposition studies for the  $[\operatorname{CrCl}_n(\operatorname{H}_2\operatorname{O})_{6-n}]^{3-n}$  and  $[\operatorname{Mn}^{2+}\operatorname{Cl}_n(\operatorname{H}_2\operatorname{O})_{6-n}]^{2-n}$  clusters [20,21], molecular water contributes more to D than to the  $\operatorname{Cl}^-$  ion. It can be shown that the centers I and II are clusters of  $[\operatorname{CrCl}_{6-n}(\operatorname{H}_2\operatorname{O})_n]^{n-3}$  with n=2

	Center I [CrCl <sub>4</sub> (H <sub>2</sub> O) <sub>2</sub> ] -			Center II [CrCl <sub>5</sub> (H <sub>2</sub> O)] <sup>2-</sup>			Center III [CrCl <sub>6</sub> ] <sup>3-</sup>		
	D	$g_{\parallel}$	$g_{\perp}$	D	$g_{\parallel}$	$g_{\perp}$	D	$g_{\parallel}$	$g_{\perp}$
Cal.	-216	1.970	1.981	-110	1.973	1.979	-26	1.976	1.977
Expta	-217	1.970	1.982	-140	1.965	1.979	-25	1.982	1.981

<sup>&</sup>lt;sup>a</sup> The signs of *D* for the three tetragonal centers were not given in [1]. However, we can reasonably assume that for all the centers the sign of *D* is negative, based on the empirical relationship  $D \approx \zeta (g_{\parallel} - g_{\perp}) / (6k)$  [23,24].

Table 1. EPR parameters D (in units of  $10^{-4}~{\rm cm}^{-1}$ ),  $g_{\parallel}$  and  $g_{\perp}$  for the three tetragonal centers I, II and III in CsCl:Cr<sup>3+</sup> crystal at room temperature.

and 1, respectively [1, 2]. Similar to (6), the tetragonal field parameter can be expressed as

$$D_{\rm t} \approx \frac{16}{21} [\bar{A}_4({\rm Cl}^-) - \bar{A}_4({\rm H_2O})]$$
 (8)

for center I and

$$D_{t} \approx \frac{8}{21} \left\{ \bar{A}_{4}(Cl^{-}) \left[ 2(R'_{0}/R'_{\perp})^{t4} - (R_{0}/R'_{\parallel})^{t4} \right] - \bar{A}_{4}(H_{2}O) \right\}$$
(9)

for center II.

In the above formulas, the reference bonding distance for center II can be written as  $R_0\prime \approx (R_\parallel\prime + 4R_\perp\prime)/5$ . Considering that the only difference between center III and center I (or II) arises from two (or one) water molecules substituting the host Cs<sup>+</sup> ion(s) along the C<sub>4</sub> axis, the metal-ligand distances  $R_\parallel$  and  $R_\perp$  in center III can be approximately adopted for the center II (i. e.,  $R_\parallel\prime \approx R_\parallel$  and  $R_\perp\prime \approx R_\perp$ ). The intrinsic parameter  $\bar{A}_4$  (H<sub>2</sub>O) equals about (3/4) $D_q$ (H<sub>2</sub>O) [15], with the cubic field splitting  $D_q$ (H<sub>2</sub>O) ( $\approx$ 1740 cm<sup>-1</sup>) for the [Cr(H<sub>2</sub>O)<sub>6</sub>]<sup>3+</sup> cluster [22]. Since there are no optical spectra available for the centers I and II, we can reasonably take the mean cubic field parameters  $D_q$ (I) and  $D_q$ (II) for the centers I and II in terms of  $D_q$  in (5) for center III, i. e.,

$$D_{\mathbf{q}}(\mathbf{I}) \approx [2D\mathbf{q}(\mathbf{C}\mathbf{I}^{-}) + D\mathbf{q}(\mathbf{H}_{2}\mathbf{O})]/3,$$

$$Dq(II) \approx [5Dq(Cl^{-}) + Dq(H_2O)]/6$$
 (10)

For simplicity, the values B and C in (5) are approximately adopted for the centers I and II.

Since the S.O. coupling parameter of  $O^{2-}$  ( $\zeta_p^0 \approx 150~cm^{-1}$  [22]) in molecular water is much smaller than that of Cl<sup>-</sup>, the contribution to the EPR parameters from the S.O. coupling parameter of molec-

[1] F.S. Stibbe and N.J. Trappenieers, Phys. B **95**, 81 (1978).

ular(s) water in centers I and II may be much smaller than that from the S.O. coupling parameter of Cl<sup>-</sup> ligands and can be ignored. So, only the five and four Cl<sup>-</sup> ions are included in the calculation of metal-ligand overlap for center I and II, respectively. Thus, we have the average group overlap integrals  $S_{\rm dp}(t_{2g}) \approx 0.01293$  and  $S_{\rm dp}(e_g) \approx 0.04158$  for the center I and  $S_{\rm dp}(t_{2g}) \approx 0.01034$  and  $S_{\rm dp}(e_g) \approx 0.03327$  for center II

By applying the above parameters in (1), the theoretical values of D,  $g_{\parallel}$  and  $g_{\perp}$  for centers I and II are calculated and shown in Table 1.

## 3. Results and Discussion

From Table 1, one finds that the calculated values of D,  $g_{\parallel}$  and  $g_{\perp}$  for the three centers agree reasonably with the observed data. By analyzing its EPR data, the local structure of center III is also determined, i.e., the two substitutional Cl<sup>-</sup> ions do not occupy exactly the host Cs<sup>+</sup> sites, but shift away from the central interstitial Cr<sup>3+</sup> ion by about 0.506 Å due to the spacial size effect along the C4 axis. Thus, the little difference between  $R_{\parallel}$  and  $R_{\perp}$  ( $\approx 2.565$  Å) and hence the very small  $D_{\rm t}~(\approx -6.1~{\rm cm}^{-1})$  can be understood for the [CrCl<sub>6</sub>]<sup>3-</sup> cluster. Interestingly, if we still assume that the two substitutional Cl<sup>-</sup> ions occupy exactly the host Cs<sup>+</sup> sites ( $\Delta Z = 0$ ,  $R_{\parallel} \approx a/2 \approx 2.055$  Å, and so  $\bar{R} \approx 2.395 \text{ Å}$ ), the calculated  $D \approx 4680 \times 10^{-4} \text{ cm}^{-1}$ would be about 180 times larger than the experimental value.

Compared with center III, the relatively larger D values for centers I and II may be due to the larger tetragonal distortions arising from the substitution of Cl<sup>-</sup>ion(s) with molecular H<sub>2</sub>O having a stronger crystal field [ $Dq(H_2O) \approx 1740 \text{ cm}^{-1}$ ] than that [ $Dq(Cl^-) \approx 1370 \text{ cm}^{-1}$ ] of the Cl<sup>-</sup> ligand.

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